

SEMESTER-III

STATISTICS MAJOR

STAT-MD-CC3-3-Th

(Statistical Inference-I)

3 Credits

THEORY

Basic concepts of Statistical Inference: population & sample, parameter & statistic, population distribution and sampling distribution. Point estimation, interval estimation and testing of hypothesis. Three useful distributions for statistical Inference: χ^2 , t and F (derivations excluded). (5)

Point Estimation: Concepts of estimation, requirements of a good estimator, notions of mean square error, unbiasedness, bias-variance trade off, best linear unbiasedness and minimum variance unbiasedness. Properties of uniformly minimum variance unbiased estimators (UMVUE). Comparison of Estimators, Efficiency. Methods of Estimation: Method of moments, method of maximum likelihood estimation and statements of their small sample properties. Point estimators of the parameters of Binomial, Poisson, and univariate Normal distributions. (15)

Elements of hypothesis testing: Null and alternative hypotheses, simple & composite hypotheses, critical region, type I and type II errors, level of significance, size, power, p-value. Exact tests and confidence intervals: classical and p-value approaches. Tests relating to Binomial and Poisson distributions, Fisher's exact test. Chi-square tests for association, homogeneity and goodness of fit. Tests of hypotheses for the parameters of normal distribution (one sample and two sample problems), paired t -test. Combination of probabilities in tests of significance. (20)

Interval Estimation: Confidence Interval and Confidence Coefficient, Exact confidence interval for mean(s) and variance(s) for one and two sample problems under the Normal set-up. (5)

List of Suggested Practical

- Maximum Likelihood Estimation.
- Estimation by the method of moments.
- Test of significance for single proportion and difference of two proportions.
- Test of significance for single Poisson mean and difference of two Poisson means.
- Chi square tests for association, homogeneity and goodness of fit.
- Test of significance and confidence intervals for single mean and difference of two means.
- Test of significance and confidence intervals for single variance and ratio of two variances.

Reference Books

- Goon, A.M., Gupta, M.K. and Dasgupta, B.: Fundamental of Statistics, Vol.1. The World Press, Kolkata.
- Goon, A.M., Gupta, M.K. & Dasgupta, B.: An Outline of Statistical Theory, Vol-1. World Press.
- Rohatgi, V. K. and Saleh, A.K. Md. E.: An Introduction to Probability and Statistics. 2nd Edn. (Reprint). John Wiley and Sons.
- Hogg, R.V., Tanis, E.A. and Zimmerman, D. L.: Probability and Statistical Inference. Pearson Education.
- Johnson, R.A. and Bhattacharya, G.K.: Statistics-Principles and Methods, 4th Edn. John Wiley and Sons.
- Mood, A.M., Graybill, F.A. and Boes, D.C.: Introduction to the Theory of Statistics, 3rd Edn. (Reprint). Tata McGraw-Hill.
- Hogg, R.V., McKean, J.W. and Craig, A.T.: Introduction to Mathematical Statistics, 8th Edition. Pearson.
- Gupta, S.C. and Kapoor, V.K. (2020): Fundamentals of Mathematical Statistics. Sultan Chand and Sons.
- Ramachandran, K.M. and Tsokos, C.P.: Mathematical Statistics with Applications. Academic Press.
- Roychowdhury, S., Bhattacharya, D.: Probability and Statistical Inference Theory and Practice, U.N. Dhur & Sons. Pvt. Ltd.

